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## Abstract

The aims of this paper are to present the background and specification of the Integrated Modelling of European Migration (IMEM) model. Currently, international migration data are collected by individual countries with separate collection systems and designs. This creates problems when attempting to understand or predict population movements between countries as the reported data are inconsistent in terms of their availability, definitions and quality. Rather than wait for countries to harmonise their migration data collection and reporting systems, we propose a model to overcome the limitations of the various data sources. In particular, we propose a Bayesian model for harmonising and correcting the inadequacies in the available data and for estimating the completely missing flows. The focus is on estimating recent international migration flows amongst countries in the European Union (EU) and European Free Trade Association (EFTA) from 2002 to 2008, using data collected by Eurostat and other national and international institutions. We also include additional information provided by experts on the effects of undercount, measurement and accuracy. The methodology is integrated and capable of providing a synthetic data base with measures of uncertainty for international migration flows and other model parameters.

## 1 Introduction

In order to fully understand the causes and consequences of international population movements in Europe, researchers and policy makers need to overcome the limitations of the various data sources, including inconsistencies in the availability, definitions and quality (Kelly 1987; Zlotnik 1987; Willekens 1994; Bilsborrow et al. 1997; Poulain et al. 2006; Kupiszewska and Nowok 2008). In this paper, we propose a Bayesian model for harmonising and correcting the inadequacies in the available data

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and for estimating the completely missing flows. The focus is on estimating recent international migration flows amongst countries in the European Union (EU) and European Free Trade Association (EFTA) from 2002 to 2008, using data collected by Eurostat and other national and international institutions. The methodology is integrated and capable of providing a synthetic data base with measures of uncertainty for international migration flows and other model parameters.

The advantages in having a consistent and reliable set of migration flows are numerous. Estimates of migration flows are needed so that governments have the means to improve their planning policies directed at supplying particular social services or at influencing levels of migration. This is important because migration is currently (and increasingly) the major factor contributing to population change. Furthermore, our understanding of how or why populations change requires reliable information about migrants. Without this, our ability to predict, control or understand that change is limited. Finally, countries are now required to provide harmonised migration flow statistics to Eurostat as part of a new regulation passed by the European Parliament in 2007. Recognising the many obstacles with existing data, Article 9 of the Regulation states that 'As part of the statistics process, scientifically based and well documented statistical estimation methods may be used.'<sup>1</sup> Our proposed framework helps countries achieve this aim and provides measures of accuracy required for understanding the estimated parameters and flows.

This paper is structured as follows. First, we provide some background and context to this work. Second, in Section 3, we specify the IMEM model, which includes a model for measurement error and a spatial interaction-type model for estimating missing migration flows. In Section 4, we describe the main sources of the data used in this paper. The construction of the priors for our model is then presented in Section 5, followed a presentation of the results. Finally, the paper concludes with a summary and a discussion.

## 2 Background

The reasons for international migration are many. People move for employment, family reunion or amenity reasons. Reported statistics on these flows, on the other hand, are relatively confusing or nonexistent. There are two main reasons. First, no consensus exists on what exactly is a "migration". Therefore, comparative analyses suffer from differing national views concerning who is a migrant. Second, the event of migration is rarely measured directly. Often it is inferred by a comparison of places of residence at two points in time or as a change in residence recorded by a population registration system. The challenge is compounded because countries use different methods of data collection. Migration statistics may come from administrative data, decennial population censuses or surveys.

The timing criterion used to identify international migrants varies considerably between countries. For population register data, international migration may refer to persons who plan to live or have lived in a different country for no minimum period, three months, six months, one year, or even more. Research is needed to reconcile the different timings used to collect or analyse migration data, as well as between different collection systems (see, e.g., de Beer et al. 2010; Nowok 2010; Nowok and Willekens forthcoming).

International migration statistics also suffer from unreliability, mainly due to

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<sup>1</sup><http://www.europarl.europa.eu/sides/getDoc.do?objRefId=140109&language=EN>.

under-registration of migrants and data coverage (Nowok et al. 2006). This is often caused by the collection method or by non-participation of the migrants themselves. In general, migration data may be unreliable because they are often based on intentions. Emigration data are particularly problematic because migrants may not notify the population register of their movement because it is not in their interest to do so. Surveys, such as the United Kingdom's International Passenger Survey, often do not have large enough sample sizes to adequately capture the needed details for analysing migration. Without a relatively large sample size, irregularities in the data are likely to appear, such as in the country-to-country-specific flows (Raymer and Bijak 2009). Furthermore, flows for certain countries may be missing for particular years or entirely. Finally, migration data may be available only for the total population, not for more detailed demographic, socioeconomic or spatial characteristics required for a particular study.

Because of all the problems associated with inconsistency and missing data, there has been a limited amount of work carried out in the area of estimating international migration matrices. Most of the estimation work has been focused on indirect methods for particular countries, independent of others (e.g., Warren and Peck 1980; Jasso and Rosenzweig 1982; Hill 1985; Zaba 1987; van der Gaag and van Wissen 2002). There are, however, several (mostly recent) efforts on estimating migration flow matrices from which we can draw experiences. First, Poulain (1993, 1999) developed a correction factor approach, using optimisation techniques, to reconcile differences between flows reported by receiving and sending countries in Europe. The calculated correction factors provided both a means for harmonising migration flows and a basis for understanding the reasons for the differences. Second, Raymer (2007, 2008) developed a hierarchical multiplicative component approach for estimating international migration flows in Europe by age and sex. The multiplicative component approach showed how log-linear models could be applied to model international migration flows in a systematic and hierarchical manner. Third, Brierley et al. (2008) extended this approach in a Bayesian context and demonstrated the usefulness and flexibility of incorporating various forms of prior information and the importance of distributions quantifying uncertainty in the estimated values. Fourth, Cohen et al. (2008) developed a gravity model to project international migration flows for all countries in the world (see also Kim and Cohen 2010). Fifth, Abel (2010) extended Poulain's optimisation methods and applied statistical methods for missing data (i.e., expectation-maximisation) to estimate flows amongst 15 European Union countries.

Finally, and most recently, researchers at the Netherlands Interdisciplinary Demographic Institute (NIDI, The Hague), the Central European Forum for Migration and Population Research (CEFMR, Warsaw), the Southampton Statistical Sciences Research Institute (S3RI) and the Université Catholique de Louvain (Charleroi) collaborated on a Eurostat-funded project to estimate international migration stocks and flows in Europe. The methodology adopted by the MIMOSA (MIgration MOdelling for Statistical Analyses) team represented a two-stage hierarchical procedure. The first stage, described in de Beer et al. (2010), harmonises the flows amongst 19 EU/EFTA countries providing both sending and receiving data by applying an extension of Poulain's (1999; see also Abel 2010) optimisation procedure benchmarked to Sweden's migration flow data, which were assumed to be measured more or less without error. The second stage, described in Raymer et al. (2011), estimates the missing marginal data and associations between countries by using the harmonised flows and covariate information. Both stages are set within a multiplicative frame-

work for analysing migration flows. No measures of uncertainty are provided and the approach is sensitive to the model assumptions and the hierarchical estimation procedure. However, the estimates produced are considered reasonable and currently represent the most extensive and comprehensive set of harmonised migration flow estimates in Europe. These estimates may be downloaded from NIDI’s website.<sup>2</sup>

The above research has led us to the conclusion that a Bayesian approach offers the best opportunity for integrating all the different types of data, covariate information and expert judgements. There are two important advantages of adopting a Bayesian approach in the context of the proposed research. First, the methodology offers a coherent and probabilistic mechanism for describing various sources of uncertainty contained in the various levels of modelling. These include the migration processes, models, model parameters and expert judgements. Second, the methodology provides a formal mechanism for the inclusion of expert judgement to supplement the deficient migration data. As noted by Willekens (1994), a Bayesian approach for modelling international migration is particularly well-suited for incorporating expert judgement to substitute for data shortages.

Applications of Bayesian methods in migration and population analyses include predictions of international migration from time series models (Gorbey et al. 1999; Bijak and Wiśniowski 2010; Bijak 2011; Mitchell et al. 2011). They have also been used to model non-migratory spatial movements (Congdon 2001), produce forecasts of fertility (Tuljapurkar and Boe 1999) and mortality (Czado et al. 2005; Girosi and King 2008; Chunn et al. 2010), and to estimate population sizes under situations of very limited information (Daponte et al. 1999). A thorough overview of applications of Bayesian methods in social sciences, including demographic modelling in the multistate framework, is offered by Lynch (2007).

### 3 Methodology

There are two key design aspects of our methodology: (1) the development of the underlying statistical framework and (2) the specification of prior information. We address each of these in turn below.

#### 3.1 The Statistical Modelling Framework

The data of interest can be conveniently expressed in a two-way contingency table or matrix showing the origin-to-destination flows with the cell counts corresponding to the number of migrants in a specified period. We observe counts (flows)  $z_{ijt}^k$  from country  $i$  to country  $j$  during year  $t$  reported by either the sending  $S$  or receiving  $R$  country, where  $k \in \{S, R\}$ . These flows can be represented by matrices  $Z_t^S$  and  $Z_t^R$ :

$$Z_t^S = \begin{pmatrix} 0 & z_{12t}^S & z_{13t}^S & \cdots & z_{1nt}^S \\ z_{21t}^S & 0 & z_{23t}^S & \cdots & z_{2nt}^S \\ z_{31t}^S & z_{32t}^S & 0 & \cdots & z_{3nt}^S \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ z_{n1t}^S & z_{n2t}^S & z_{n3t}^S & \cdots & 0 \end{pmatrix} \quad Z_t^R = \begin{pmatrix} 0 & z_{12t}^R & z_{13t}^R & \cdots & z_{1nt}^R \\ z_{21t}^R & 0 & z_{23t}^R & \cdots & z_{2nt}^R \\ z_{31t}^R & z_{32t}^R & 0 & \cdots & z_{3nt}^R \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ z_{n1t}^R & z_{n2t}^R & z_{n3t}^R & \cdots & 0 \end{pmatrix}.$$

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<sup>2</sup><http://www.nidi.nl/Pages/NID/24/928.bGFuZz1VSw.html>.

The interest of this research is to estimate a matrix  $Y_t$  of true migration flows with unknown entries:

$$Y_t = \begin{pmatrix} 0 & y_{12t} & y_{13t} & \cdots & y_{1nt} \\ y_{21t} & 0 & y_{23t} & \cdots & y_{2nt} \\ y_{31t} & y_{32t} & 0 & \cdots & y_{3nt} \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ y_{n1t} & y_{n2t} & y_{n3t} & \cdots & 0 \end{pmatrix}.$$

For all  $i, j$  and  $t$ , we assume that  $z_{ijt}^k$  follows a Poisson distribution

$$z_{ijt}^S \sim \text{Po}(\mu_{ijt}^S), \quad (1)$$

$$z_{ijt}^R \sim \text{Po}(\mu_{ijt}^R). \quad (2)$$

### 3.2 Measurement error model

In our model,  $y_{ijt}$  is a true flow of migration from country  $i$  to country  $j$  in year  $t$ . It includes migration flows to and from rest of world (category  $i = 0$ ). In terms of measurement, true flows are consistent with the United Nations (UN, 1998) recommendation for long-term international migration, that is a **long-term migrant** is *a person who moves to a country other than that of his or her usual residence for a period of at least a year (12 months), so that the country of destination effectively becomes his or her new country of usual residence.*

The two measurement error equations are

$$\log \mu_{ijt}^S = \log y_{ijt} + \psi_i - \log(1 + e^{-\kappa_i}) + \varepsilon_{ijt}^S, \quad (3)$$

$$\log \mu_{ijt}^R = \log y_{ijt} + \gamma_j - \log(1 + e^{-\kappa_j}) + \varepsilon_{ijt}^R, \quad (4)$$

where we assume  $\varepsilon_{ijt}^S \sim \mathcal{N}(0, \tau_i^S)$  and  $\varepsilon_{ijt}^R \sim \mathcal{N}(0, \tau_j^R)$ . The precisions (reciprocal variances) of the error terms depend on whether the data are captured by sending or receiving countries. Thus we take

$$\tau_i^S = t_{c(i)}^S, \quad (5)$$

$$\tau_j^R = t_{c(j)}^R, \quad (6)$$

where  $c(i)$  denotes the type of collection system (e.g., population register or survey). The number of parameters required to capture differences in accuracy, ultimately depends on our typology of collection systems, and their relative ability to capture migration flows, regardless of definition and coverage. For the moment,  $c(i)$  is the same for all countries. The accuracy is only distinct for emigration and immigration.

The differences in duration of stay criterion, which depend on the reporting country, and the effect of undercount are captured by the parameters  $\psi_i$  and  $\gamma_j$ ,

$$\psi_i = \begin{cases} \delta_1 + \log \lambda_1 & \text{if duration is 0 months} \\ \delta_2 + \log \lambda_1 & \text{if duration is 3 months} \\ \delta_3 + \log \lambda_1 & \text{if duration is 6 months} \\ \log \lambda_1 & \text{if duration is 12 months} \\ \delta_4 + \log \lambda_1 & \text{if duration is permanent} \end{cases}, \quad (7)$$

$$\gamma_j = \begin{cases} \delta_1 + \log \lambda_2 & \text{if duration is 0 months} \\ \delta_2 + \log \lambda_2 & \text{if duration is 3 months} \\ \delta_3 + \log \lambda_2 & \text{if duration is 6 months} \\ \log \lambda_2 & \text{if duration is 12 months} \\ \delta_4 + \log \lambda_2 & \text{if duration is permanent} \end{cases}. \quad (8)$$

The  $\delta_m$  parameter measures the effect of a particular duration of stay definition used by country  $i$ . The parameters are constrained so that  $\delta_1 > \delta_2 > \delta_3 > 0$  and  $\delta_4 < 0$  in the following way,

$$\begin{aligned}\delta_1 &= d_1 + d_2 + d_3, \\ \delta_2 &= d_2 + d_3, \\ \delta_3 &= d_3, \\ \delta_4 &= -d_4,\end{aligned}$$

where  $d_k > 0$  are auxiliary parameters. The  $\lambda_r$  parameters measure the effect of the undercount with the assumption that  $\lambda_r \in (0, 1)$ .

Finally, the  $\kappa_i$  parameter is a normally distributed country-specific random effect

$$\kappa_i \sim \mathcal{N}(\nu_i, \zeta_i),$$

where  $\nu_i = \nu_{m(i)}$  is a group-specific mean and  $\zeta_i = \zeta_{m(i)}$  is a group-specific precision and  $m(i)$  denotes a type of coverage assumed for country  $i$ . For the time being, there are two coverage types, that is,  $m(i) \in \{\text{standard}, \text{excellent}\}$ . The logistic transformation of  $\kappa$  in Equations 3 and 4 ensures that the function is bounded within a range  $(0, 1)$  on the linear scale. It can be interpreted in terms of the differences in coverage with respect to the UN definition of migration.

For the migration to and from the rest of world there is only one equation per outflow and inflow, respectively, i.e.,

$$\begin{aligned}\log \mu_{i0t}^S &= \log y_{i0t} + \psi_i + \varepsilon_{i0t}^S, & \text{for all } i \text{ and } t & \quad (9) \\ \log \mu_{0jt}^R &= \log y_{0jt} + \gamma_j + \varepsilon_{0jt}^R, & \text{for all } j \text{ and } t, & \quad (10)\end{aligned}$$

All other parameters remain same as described above, except for  $\psi_i$  and  $\gamma_j$ , which are defined as in Equations 7 and 8 with  $\lambda_1$  and  $\lambda_2$  replaced with  $\lambda_3$  and  $\lambda_4$ , respectively. Note, that in the measurement of the flows to and from the rest of world we assume a perfect coverage for all countries, i.e., there are no country-specific random effects.

### 3.3 Migration model

The true flows of migration may be modelled according to a set of covariate information. Here, we rely on migration theory and empirical evidence to drive the development of the model (see, e.g., Jennissen 2004; Abel 2010; Raymer et al. 2011). The explanatory variables can be grouped into economic, demographic and geographic ones. Consider the following model of migration:

$$\begin{aligned}\log y_{ijt} &= \alpha_1 + \alpha_2 \log(P_{it}) + \alpha_3 \log(P_{jt}) + \alpha_4 C_{ij} + \alpha_5 \log(T_{ijt}) + \\ &\quad \alpha_6 \log(G_{it}/G_{jt}) + \alpha_7 A_{ijt} + \alpha_8 (S_{ij}) + \xi_{ijt},\end{aligned} \quad (11)$$

where  $\alpha = (\alpha_1, \dots, \alpha_8)'$  is a vector of parameters. The random term  $\xi$  is assumed to be normally distributed with 0 mean and constant precision  $\tau_y$ , following Brierley et al. (2008).

The following set of covariates is used:

1. The mid-year populations (averages of 1 January populations of subsequent years) in sending and receiving country, denoted as  $P_{it}$  and  $P_{jt}$ ; source: NewCronos database of Eurostat.

2. Dummy variable indicating contiguity (or neighbouring countries) with 1 if countries  $i$  and  $j$  have a common border and 0 otherwise,  $C_{ij}$ ; source: Mayer and Zignago (2006). Contiguity between all Scandinavian countries are assumed.
3. The ratio of the Gross National Income per capita in sending and receiving countries,  $G_{it}/G_{jt}$ ; source: World Development Indicators (2010).
4. International trade between origin and destination countries expressed as import in current USD,  $T_{ijt}$ ; source: UN Commodity Statistics Database <sup>3</sup>.
5. Dummy variable for accession  $A_{ijt}$ . It is equal to 1 for the flows between ten countries which joined the EU in 2004 and Ireland, the United Kingdom and Sweden, i.e., the countries that did not restrict their labour to these movements during the years 2004-2008.
6. Origin-destination migrant stocks based on the 2000 population censuses round,  $S_{ij}$ ; source: Parsons et al. (2005).

All non-indicator variables were divided by their means and then logged (migrant stocks are in levels due to zero entries in the data).<sup>4</sup>

For modelling flows to the rest of world, we use a model with additional covariates based on Raymer et al. (2011).

$$\log y_{i0t} = \beta_1 + \beta_2 \log(P_{it}) + \beta_3 \log(G_{it}) + \beta_4 H_i + \beta_5 \log(S_{0i}) + \beta_6 \log(E_{it}) + \beta_7 \log(L_{it}) + \xi_{i0t}, \quad (12)$$

and for flows from the rest of world

$$\log y_{0jt} = \beta_8 + \beta_9 \log(P_{jt}) + \beta_{10} \log(G_{jt}) + \beta_{11} H_j + \beta_{12} \log(S_{0j}) + \beta_{13} \log(E_{jt}) + \beta_{14} \log(L_{jt}) + \xi_{0jt}. \quad (13)$$

The errors,  $\xi_{i0t}$  and  $\xi_{0jt}$ , are normally distributed with mean zero and precisions  $\tau_{0S}$  and  $\tau_{0R}$ , respectively. The additional covariates are

1. A dummy indicating if the country was a member of the Schengen agreement as of 1 January 2007,  $H_i$ .
2. Stocks of migrants born outside the EU and the EFTA countries,  $S_{0i}$  and  $S_{0j}$ ; source: Parsons et al. (2005).
3. Share of the population older than 65 years,  $E_{it}$ ; source: Population Reference Bureau's World Population Data Sheet 2002-2008<sup>5</sup>.
4. Life expectancy at birth of women in years,  $L_{jt}$ ; source: Population Reference Bureau's World Population Data Sheet 2002-2008<sup>6</sup>.

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<sup>3</sup><http://comtrade.un.org>, accessed July 2010

<sup>4</sup>For Liechtenstein the following imputations were carried out: (1) GNIs per capita were assumed the same as in Switzerland (CH); (2) Trade flows are taken from the statistical office's website, <http://www.llv.li>, accessed July 2010, and converted from CHF to USD. Exports from Liechtenstein to other countries was approximated. Trade between LI and CH is calculated using ratios as presented in 'Liechtenstein - Industrial location', <http://www.liechtenstein.li/en/>, accessed July 2010, with the result that exports from LI to CH was estimated to be 11% of the total and the imports from CH to LI to be 33% of the total.

<sup>5</sup><http://www.prb.org>, accessed February 2010

<sup>6</sup><http://www.prb.org>, accessed February 2010



## 4 Data Collection

For this study, we collected as much data as we could on the migration flows amongst the 31 countries in the EU and EFTA from 2002 to 2008.<sup>7</sup> Our model includes flows to and from rest of world, which is needed to obtain the total immigration and emigration flows for each country. In the future, we hope to extend the modelling to include age, sex and the year 2009, for which some data are starting to become available (at the time of this writing).

The migration flow data used in the project comes primarily from the Eurostat data base, which relies on the annual Joint Questionnaire on Migration Statistics sent to all national statistical agencies in the European Union. This questionnaire is coordinated by the Council of Europe, the United Nations Statistical Division, the United Nations Economic Commission for Europe and the International Labour Organization. In some cases, we obtained additional information from websites organised and maintained by national statistical agencies. Furthermore, as described in the previous section, we collected covariate information for use in the migration model to estimate missing flows.

Before constructing the model, we spent a lot of time trying to understand the country-specific measurements underlying the reported statistics. Here, we relied heavily on Poulain et al. (2006), two MIMOSA reports (Kupiszewska and Wiśniowski 2009; van der Erf 2009) and our own analyses (van der Erf 2010). We found that no two countries used the same collection system and often different conceptualisations of migration are utilised. In many cases, these conceptualisations differed within countries, depending on whether the migrant was a foreigner, EU/EFTA member or national of the sending or receiving country.

## 5 Constructing the priors

In order to produce realistic and meaningful estimates of migration flows, expert opinions are required. The Bayesian approach permits expert opinion to be combined with the data to strengthen the inference. For this study, we sought expert information on undercount, effects of duration and accuracy of migration data collection systems for the purpose of informing our priors for the measurement model. The Bayesian approach also facilitates the combination of multiple data sources, with their differing levels of error, as well as prior information about the structures of the migration processes, into a single prediction with an associated measure of uncertainty.

The priors for duration of stay, undercount and precision are elicited from the experts by means of a Delphi survey (see Wiśniowski et al. 2011). For the duration of stay parameters,  $\delta_1$ ,  $\delta_2$  and  $\delta_3$ , we assume a mixture of log-normal priors for auxiliary parameters  $d_k$ , which were obtained from the experts. The resulting interquartile ranges and medians for the mixtures are presented in Table 1. The interpretation of these priors is straightforward. For example, consider the median of six months duration parameter,  $\delta_3$ , which is equal to 1.22. This value implies that flows measured by using a six-month duration are expected to be 22% larger than the corresponding true flows measured with a 12 month duration criterion. Note that the prior for  $\delta_4$

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<sup>7</sup>The following assumptions with respect to the data have been made: (1) For the Netherlands - category 'Unknown' in the data on emigration was distributed proportionally to all the countries; (2) Category 'ex-Czechoslovakia' in the migration from and to Denmark was distributed to the Czech Republic and Slovakia proportionally for each year.

(permanent duration) was not elicited from the experts. Instead, the prior for its auxiliary parameter  $d_4$  was assumed to be

$$d_4 \sim \log \mathcal{N}(-0.5, 30),$$

which for  $\delta_4$  implies an interquartile range of (0.50, 0.59) and a median of 0.55.

Table 1: Characteristics of the expert-based priors for duration of stay parameters

	$q(0.25)$	median	$q(0.75)$
$\delta_1$	1.86	2.22	2.82
$\delta_2$	1.42	1.65	2.03
$\delta_3$	1.13	1.22	1.39

The priors for the undercount parameters  $\lambda_r$  are mixtures of beta densities resulting from the experts' opinions about undercount (see Wiśniowski et al. 2011). Their characteristics are presented in Table 2.

Table 2: Characteristics of the expert-based priors for undercount parameters

	$q(0.25)$	median	$q(0.75)$
$\lambda_1$	0.39	0.56	0.73
$\lambda_2$	0.61	0.76	0.85
$\lambda_3$	0.33	0.54	0.72
$\lambda_4$	0.45	0.63	0.77

The prior densities for the precision of the error terms in the measurement equations were also obtained from experts, and then combined into mixtures of gamma densities. Due to the heterogeneity of expert's judgements the resulting priors are rather vague with interquartile ranges of (14, 982) for emigration and (210, 1373) for immigration, and with medians of 551 and 877, respectively. The medians deviated from the average levels by  $\pm 4.3\%$  and  $\pm 3.4\%$ , respectively.

The coverage random effects parameters,  $\kappa_i$ , for countries with excellent coverage (i.e., DK, FI, NL, NO, SE) are assumed fixed and equal to zero on the log scale. Hence, the resulting scaling factor for the true flows is equal to 1. For the rest of the countries, with standard coverage, we assume the following

$$\kappa_i \sim \mathcal{N}(\nu_{m(i)}, \zeta_{m(i)}), \quad \text{for } m(i) = \text{standard},$$

where

$$\nu_i \sim \mathcal{N}(1, 0.5),$$

and

$$\zeta_i \sim \mathcal{G}(4, 1).$$

These priors imply the coverage random effects characteristics to be as in Table 3. This (subjective) specification is based on the experiences in the MIMOSA project.

Table 3: Characteristics of the priors for random parameters

	$q(0.25)$	median	$q(0.75)$
standard coverage	0.26	0.50	0.74

Finally, for the constants in the migration models for intra-European flows, a normal hierarchical prior is assumed

$$\alpha_1 \sim \mathcal{N}(0, \tau_\alpha),$$

$$\tau_\alpha = 1/a^2, \quad a \sim \mathcal{U}(1, 10).$$

The same priors for the constants in the model for flows amongst EU/EFTA countries and the rest of world are used. This prior reduces the autocorrelation of the MCMC sample greatly and allows for faster convergence of the algorithm. For the rest of the parameters in the migration models, weakly informative normal priors,  $\mathcal{N}(0, 0.1)$ , are assumed. For the precision in the migration models, we assume a gamma prior density  $\mathcal{G}(1, 1)$ .

## 6 Results

The IMEM model was developed in the OpenBUGS software dedicated to Bayesian computations. The posterior characteristics were computed with MCMC samples of 10,000. The MCMC is a numerical method allowing us to simulate samples, which, in turn are used to reconstruct the marginal posterior density of any parameter of interest.

The posterior means of the duration of stay factors, which are defined as  $\exp(-\delta_k)$ , are presented in Table 4. We can interpret them as a multiplicative adjustment factor in the equation *true flow* = *factor* × *data*. Our benchmark criterion of 12 months produces a factor equal to one. For countries with a ‘no time limit’ of stay criterion, the true flows constitute 53% of the observed data. For six months, this factor is 74%. For permanent duration the true flows are on average twice larger than the observed data. The posterior densities of the duration of stay factors are presented in Figure 1.

Table 4: Posterior characteristics of the duration criteria factors

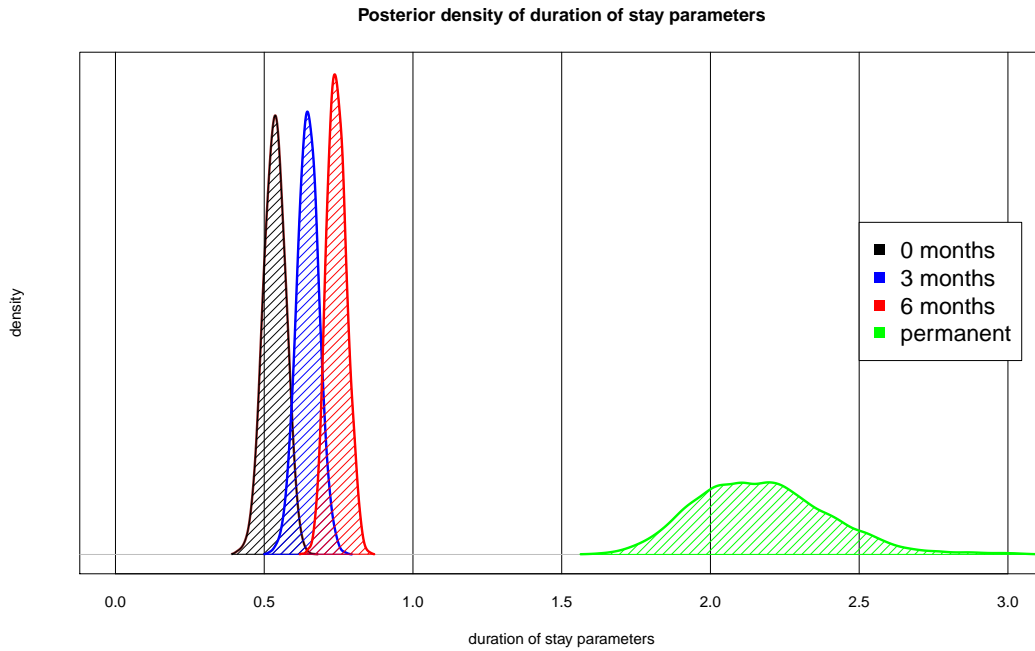
duration	no time limit	3 months	6 months	<b>12 months</b>	permanent
mean	53%	65%	74%	<b>100%</b>	218%
std.dev	3.6%	3.7%	3.3%	NA	22.5%

Source: own computations

Within the EU and EFTA, the undercount of flows is estimated to be 56% on average (standard deviation 5.0%) for emigrants and 79.6% on average (with standard deviation 6.9%) for immigrants. That is, the observed emigration data constitute 56% and 79.6%, respectively, of the true flows. The estimated undercount of emigration to the rest of the world is estimated to be 45.5% of the true flows (with standard deviation 13.8%). The corresponding figure for immigration from the rest of world is 51.6% (with standard deviation 13.0%). As the identification of undercount parameters are not possible from the data alone, these expert-based priors were particularly informative for our model.

The ultimate aim of this research is to produce posterior distributions of all the true flows amongst the 31 countries from 2002 to 2008. In Table 5 and Figure 2, we present posterior characteristics and densities of the 2006 flows from Denmark to The Netherlands and from France to Hungary. For the Denmark to The Netherlands flow, both countries provided data, resulting in a prior that is comparatively tight, with mean around 740 people. For the flow from France to Hungary, on the other

Figure 1: Posterior densities of the duration criteria parameters



hand, neither country provided data. Here, the posterior density is based primarily on the migration model. This flow is characterised by a relatively large amount of uncertainty and a heavy right tail.

Table 5: Posterior characteristics of the migration true flows

flow	mean	std.dev	median
DK-NL	741	431	641
FR-HU	2,094	2,677	1,325

Source: own computations

As another illustration, consider the 2006 flows from Poland to Germany and from Finland to Sweden presented in Table 6 and Figures 3 and 4, respectively. The posterior true flow from Poland to Germany (Figure 3) is 152,000 people with standard deviation about 96,000. Here, the reported data, also shown in the figure, differ considerably from our estimated true flows. In fact, they are at the two opposite ‘ends’ of the distribution. The reason for this has to do with Poland and Germany’s duration of stay criteria used to identify migrants. Poland uses a permanent duration, which results in a relatively small number of migrants recorded (around 15,000). This number is additionally lowered in our model due to the undercount of emigration. In the German data collection system no time limit is applied for incoming flows. This results in a relatively large number of immigrants (around 164,000).

Table 6: Posterior characteristics of the migration true flows

flow	mean	std.dev	median
PL-DE	152,300	95,950	129,200
FI-SE	4,873	2,809	4,196

Source: own computations

Figure 2: Posterior densities of the migration true flows

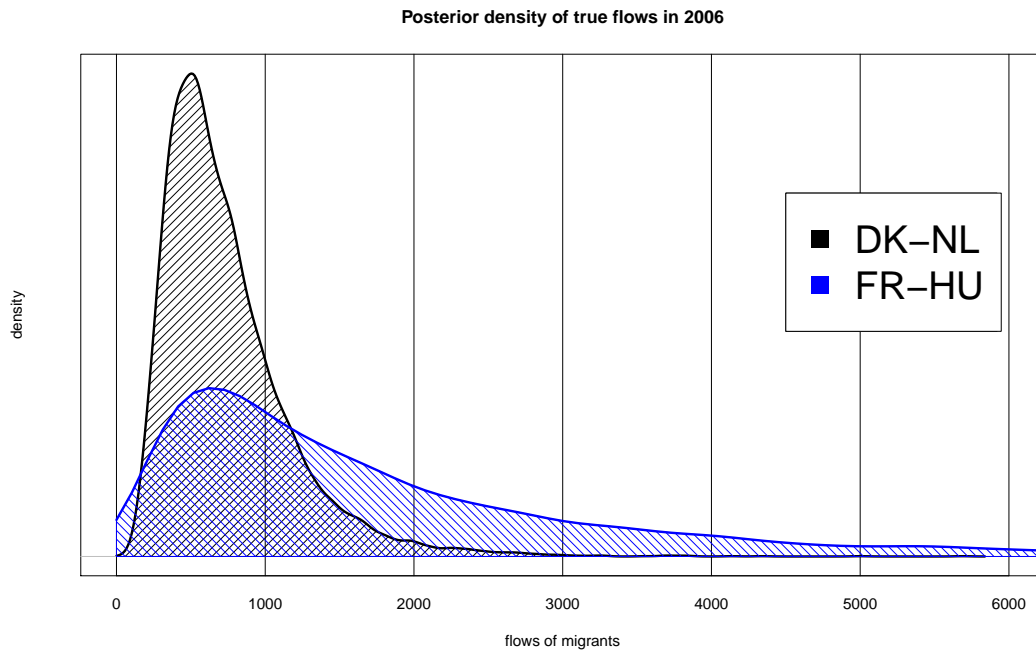
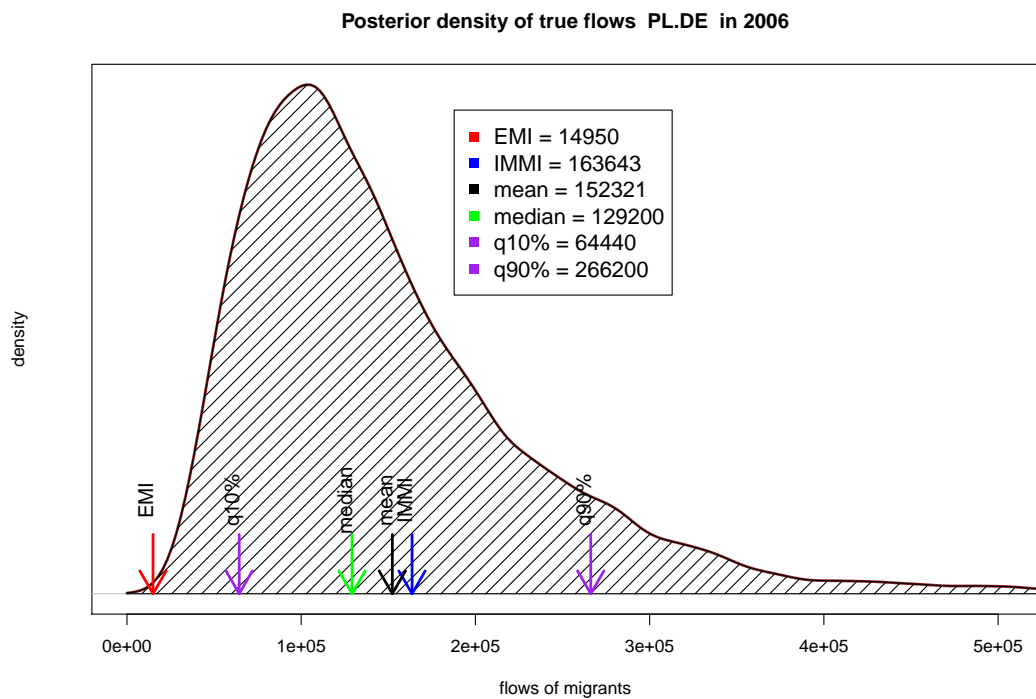
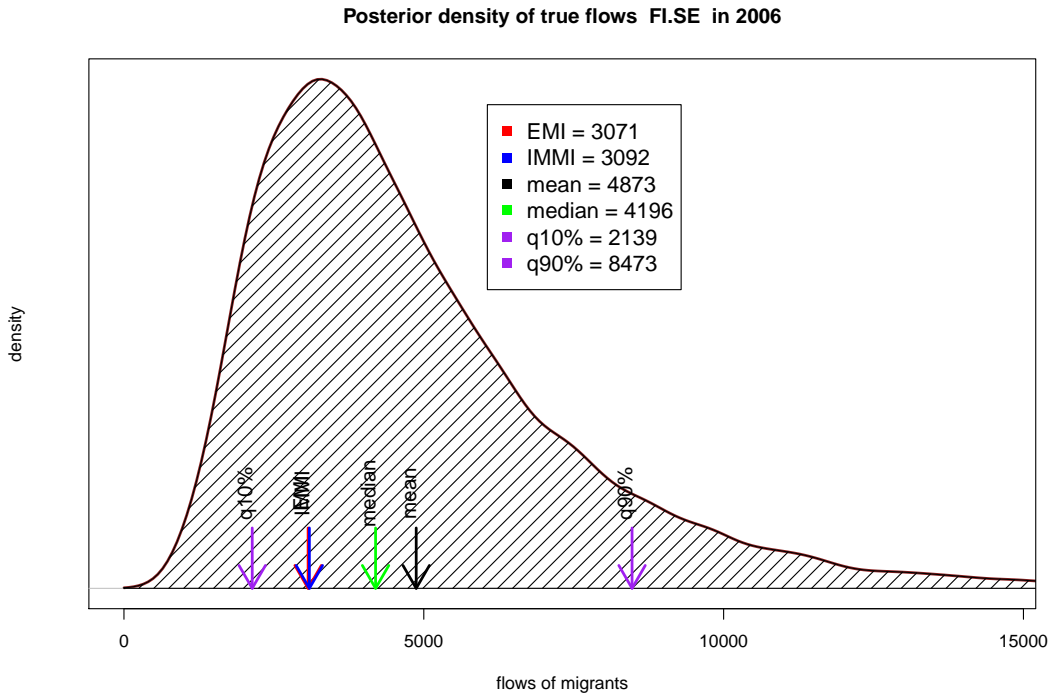


Figure 3: Posterior densities of the migration true flows



In Figure 4, a posterior density of the 2006 migration flow from Finland to Sweden is presented. The mean is around 4,900 migrants with standard deviation of around 2,800. We also observe that the data reported by both sending and receiving countries are very close to each other (around 3,000). Both reported flows lie within a range of the highest posterior density but they seem to be significantly lower than the mean or median of the posterior true flow. The reason for this is due to our inclusion of expert information on the undercount of immigration and emigration. In the MIMOSA project, Sweden’s immigration data represented the benchmark

Figure 4: Posterior densities of the migration true flows



and was assumed to be measured without error or undercount. In the IMEM model, however, the subjective expert assessment of the immigration undercount by means of a prior density on  $\lambda_2$  is incorporated. This leads to higher average flows than reported by the receiving countries.

## 7 Conclusions

In this paper, we have presented the IMEM model, which brings together empirical data, covariate information and expert judgements in a Bayesian modelling framework to estimate migration flows amongst 31 countries in Europe from 2002 to 2008. The covariate information was used to estimate missing flows. The expert judgements were used to inform the measurement model and to overcome the limitations in the existing data. While there is still some work to be done to improve the estimates and measures of uncertainty, overall we believe the model is producing reasonable and informative results. The next steps for this research are to include more detail concerning the accuracy of reported migration flows and to extend the model to include age and sex.

To conclude, we hope this work provides an important foundation for both modelling and understanding international migration, particularly in situations where the data are inadequate or missing. We have shown how data obtained from multiple sources with different measurements and collection systems can be combined together to provide a more complete and consistent picture of international migration.

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